

# Stieltjes-Wigert Polynomials and the $q$ -Airy Function

Y. T. Li and R. Wong\*

## Abstract

Asymptotic formulas are derived for the Stieltjes-Wigert polynomials  $S_n(z; q)$  in the complex plane, with the  $q$ -Airy function  $A_q(z)$  being used as the approximant. One formula holds in any disc centered at the origin, and the other holds outside any smaller disc centered at the origin; the two regions together cover the whole plane. For  $x > 1/4$ , a limiting relation is also established between the  $q$ -Airy function  $A_q(x)$  and the ordinary Airy function  $\text{Ai}(x)$  as  $q \rightarrow 1$ .

---

\*The speaker.