

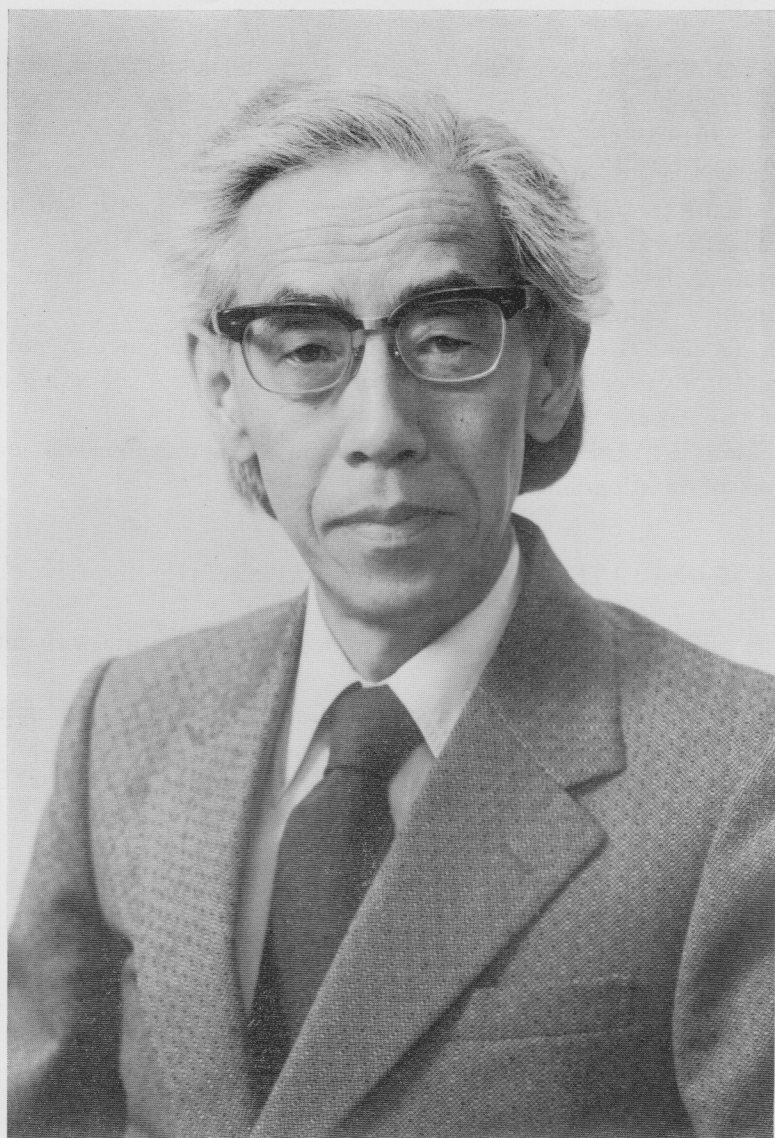
List of Contributed Papers

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- Hirōki TANABE: Linear Volterra integral equations of parabolic type
Howard JACOBOWITZ & Francois TREVES: Aberrant CR Structures
Daisuke FUJIWARA & Hideki OMORI: An example of a globally hypo-
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Taira SHIROTA

DEDICATION

Professor Taira Shirota celebrated his sixtieth anniversary on November 1st, 1982. His friends and admirers heartily expressed their joy to this occasion, and some contributed papers. The present issue of the Hokkaido Mathematical Journal, fully dedicated to Professor Shirota, is an outcome of such acts.

Shirota is originally a disciple of Professor Hidetaka Terasaka at Osaka University and started his research career in the field of Topology. It is in this period that Shirota studied topological linear spaces and contributed to the theory, by presenting several, now well-known, counter-examples. However, soon after, he was introduced to the study of partial differential equations by professor Mitio Nagumo. Shirota was then mainly interested in the general theory of linear partial differential operators, such as uniqueness and well-posedness of the Cauchy problem, propagation of regularities and related topics. Shirota's methods are since then characterized by his clear insight and his keen sense to new techniques, free from classical routines.

Shirota is more or less of the same generation as Professor Sigeru Mizohata and Masaya Yamaguti. In 1950's and early 1960's when Shirota was in Osaka while Mizohata and Yamaguti in Kyoto, researches of general linear partial differential operators in Japan were first blossomed. Shirota then moved to Hokkaido University, and assumed there one of the most famous Chairs of Analysis in Japan. Actually in his office is kept a divan, lying on which the late Professor Kiyoshi Oka, on his visit to Sapporo over some forty years ago, had got one of his genial ideas in the function theory of several complex variables.

In Sapporo, Shirota began to study systematically hyperbolic mixed, i. e., initial-boundary value, problems. With his close collaborators, he, first though in a rather involved way, characterized well-posedness of the problem in the constant coefficient case. Here they relied on, and thus revived, the classical idea of the reflection coefficients. Meanwhile, Shirota, in particular, determined propagation of analyticity for a certain class of hyperbolic mixed problems. His school also attacked the variable coefficient case and their results are now widely known. Through his activities, Shirota acquired friends abroad, and he spent a year in Nice invited by Professor Jacques Chazarain. Shirota now extends his study to certain non-linear problems arising in fluid dynamics, applying to these problems his previously obtained results and methods in linear hyperbolic mixed problems.

Since some years Shirota has organized a meeting in Sapporo every summer. From Osaka, Kyoto, Tokyo or other places come active researchers working in partial differential equations and in neighboring fields. At every meeting, originality of themes makes participants deeply satisfied, and Shirota's candid hospitality is particularly appreciated.

According to the Oriental Calendar, to each year are assigned one of Twelve Beasts of Oriental Zodiac and either "younger" or "elder" part of one of Five Elements. Since 60 is the least common multiple of 12 and 10, everyone is supposed to return to a newly born child on his sixtieth anniversary.

We wish Professor Shirota still strengthens his present vigor in his researches and in other activities, by adding a newly born baby's vivacity and vitality.

Rentaro Agemi

Koji Kubota

Atsushi Yoshikawa

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smoothness conditions. In order that the integral in (1.1) exists as a Bochner integral it was assumed that $\|A(t)\| \in O(1)$ for some $0 < t < 1$.

They also constructed the fundamental solution $W(t, \tau)$ which is an operator valued function satisfying

$$W_t(t, \tau) = A(t)W(t, \tau), \quad W(t, t) = I, \quad (1.2)$$

in some sense. The fundamental solution constructed in [2] is not a bounded operator but has the form $W(t, \tau) = W_0(t, \tau) + A(t)$ with some bounded operator $W_0(t, \tau)$ for any $t \in (0, 1)$.

In this paper using the idea of Crandall-Nehari [1], we transform (1.1) to the initial value problem of the evolution equation

$$u_t(t, x) + G(t, x)u(t, x) = G_0(t, x)u(t, x) - A(t)u(t, x), \quad (1.3)$$

where G is some mapping defined on $X(0, 1) \times X$. This problem has a solution for any initial value $u(0) \in X$. In general for the solution u of (1.3) the integral of (1.1) does not exist in the sense of Bochner integral since $\|A(t)u(t)\| = O(t^{-1})$ as $t \rightarrow 0$. However, it will be shown that if we interpret it as the improper integral

$$\lim_{\epsilon \rightarrow 0} \int_{\epsilon}^1 A(t-\tau)A(\tau)u(\tau) d\tau,$$

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